#### NONLOCALITY IN QUANTUM PHYSICS AND BEYOND

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Grenoble Nov 2012

#### 1. WHAT IS NONLOCALITY

#### 2. ENTANGLEMENT VS NONLOCALITY

#### 3. SUPER-ACTIVATION OF NONLOCALITY

#### 4. EPR STEERING

#### 5. DEVICE-INDEPENDENT QIP

#### 6. EXPERIMENTS

#### 7. NONLOCALITY BEYOND QM

#### CORRELATIONS

#### ALICE (Geneva)



#### BOB (Grenoble)



#### CORRELATIONS

ALICE (Geneva)











#### CORRELATIONS

ALICE (Geneva)

#### BOB (Grenoble)





#### **HOW DOES IT WORK?**

#### **CLASSICAL CORRELATIONS**

ALICE (Geneva)

BOB (Grenoble)



#### **CLASSICAL CORRELATIONS**

ALICE (Geneva)

BOB (Grenoble)







#### **CLASSICAL CORRELATIONS**

ALICE (Geneva)

BOB (Grenoble)



#### DEVICES HAVE A COMMON STRATEGY

#### **PRE-ESTABLISHED** CORRELATIONS



ALICE (Geneva)







#### DEVICES HAVE A COMMON STRATEGY

#### **PRE-ESTABLISHED** CORRELATIONS

**CAN THIS BE TESTED?** 



#### TWO QUESTIONS $X_0$ or $X_1$ (Alice) $Y_0$ or $Y_1$ (Bob) TWO ANSWERS +1 or -1



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#### TWO QUESTIONS $X_0$ or $X_1$ (Alice) $Y_0$ or $Y_1$ (Bob) TWO ANSWERS +1 or -1



#### Score $\leq \frac{3}{4}$ FOR ANY CLASSICAL STRATEGY

#### CHSH BELL INEQUALITY



Correlation function:  $E(X_0, Y_1) = P(X_0 = Y_1) - \frac{P}{E}(X_0 \neq Y_1)$ 

Clauser-Horne-Shimony-Holt 69

#### CHSH BELL INEQUALITY



Correlation function:  $E(X_0, Y_1) = P(X_0 = Y_1) - \frac{P}{E}(X_0 \neq Y_1)$ 

 $CHSH = E(X_0, Y_0) + E(X_0, Y_1) + E(X_1, Y_0) - E(X_1, Y_1) \le 2$ 

Clauser-Horne-Shimony-Holt 69



**LOCALITY:**  $P(a,b|x,y) = \int d\lambda P(a|x,\lambda) P(b|y,\lambda)$ 





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LOCAL CORRELATIONS SATISFY ALL BELL INEQUALITIES



**LOCALITY:**  $P(a,b|x,y) = \int d\lambda P(a|x,\lambda) P(b|y,\lambda)$ 

LOCAL CORRELATIONS SATISFY ALL BELL INEQUALITIES VIOLATION OF BELL INEQUALITY - NONLOCALITY

**BELL 64** 



#### **QUANTUM STATEGY**

## 



#### **QUANTUM STATEGY**

- 1. ENTANGLED STATE  $|\Psi\rangle = |0,1\rangle |1,0\rangle$
- 2. LOCAL MEAS  $X_0 = \vec{z} \quad X_1 = \vec{x}$  and  $Y_0 = -\vec{x} \cdot \vec{z} \quad Y_1 = \vec{x} \cdot \vec{z}$



## QUANTUM STATEGY 1. ENTANGLED STATE $|\Psi\rangle = |0,1\rangle - |1,0\rangle$ 2. LOCAL MEAS $X_0 = \vec{z}$ $X_1 = \vec{x}$ and $Y_0 = -\vec{x} \cdot \vec{z}$ $Y_1 = \vec{x} \cdot \vec{z}$ $\vec{E}(\vec{a},\vec{b}) = \langle \Psi | \vec{a} \ \vec{b} | \Psi \rangle = -\vec{a} \ \vec{b}$

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## USING QUANTUM RESOURCES ALICE $|\Psi\rangle$ BOB

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QUANTUM NONLOCALITY

#### ANY THEORY SATISFYING LOCALITY IS INCOMPATIBLE WITH QUANTUM MECHANICS

#### STRONGER THAN ANY LOCAL CORRELATIONS





#### QUANTUM NONLOCALITY

#### ENTANGLEMENT VS NONLOCALITY

#### **CONCEPTUAL DIFFERENCE**

**ENTANGLEMENT** 

NONLOCALITY

CONCEPT OF QUANTUM MECHANICS **BASED ON STATISTICS** 

MODEL INDEPENDENT

HOW TO COMPARE THEM?

#### ENTANGLEMENT = Q NONLOCALITY ?

**ENTANGLEMENT** 



QUANTUM NONLOCALITY

#### ENTANGLEMENT = Q NONLOCALITY ?

#### **ENTANGLEMENT**



#### QUANTUM NONLOCALITY
## ENTANGLEMENT = Q NONLOCALITY ?

#### **ENTANGLEMENT**



#### QUANTUM NONLOCALITY

**Q** STATE

Q STATE + MEAS.

## ENTANGLEMENT = Q NONLOCALITY ?



#### DO ALL ENTANGLED STATE VIOLATE A BELL INEQUALITY?

#### **PURE STATES**





QUANTUM NONLOCALITY

## GISIN 1991 2 PARTIES

POPESCU-ROHRLICH 1992 N PARTIES

#### **ENTANGLEMENT**



#### QUANTUM NONLOCALITY

**ENTANGLEMENT** 



QUANTUM NONLOCALITY

## THERE EXIST MIXED ENTANGLED STATE WHICH ARE LOCAL

PROJECTIVE MEAS. POVMs

WERNER 1989

**BARRETT 2002** 

**ENTANGLEMENT** 



QUANTUM NONLOCALITY

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Werner states  $\rho = \rho |\Psi > \langle \Psi | + (1-p) |/4$ 



**ENTANGLEMENT** 



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## MORE GENERAL SCENARIO





MULTIPLE COPIES CAN BE PROCESSED JOINTLY



## MORE GENERAL SCENARIO





MULTIPLE COPIES CAN BE PROCESSED JOINTLY





## SUPER-ACTIVATION OF NONLOCALITY





0 + ... + 0 **>** 0

0

PALAZUELOS PRL 2012

PALAZUELOS PRL 2012

0



#### NONLOCALITY IS SUPER-ADDITIVE



**ENTANGLED MEASUREMENTS** 





## NONLOCALITY AND TELEPORTATION



#### LARGE CLASS OF ENTANGLED STATES



CAVALCANTI, ACIN, NB, VERTESI arxiv 2012

## IS ENTANGLEMENT = NONLOCALITY ?

#### **PERES CONJECTURE (1999):** BOUND ENTANGLED STATES ARE LOCAL

**BIPARTITE CASE ?** 



VERTESI & NB PRL 2012

#### **BACK TO SCHRODINGER (1935)**

#### **BACK TO SCHRODINGER (1935)**



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#### **BACK TO SCHRODINGER (1935)**

#### BY PERFORMING A LOCAL MEASUREMENT ALICE CAN STEER THE STATE OF BOB



~ REMOTE STATE PREPARATION

#### STEERING AS INFORMATION TASK

#### DISTRIBUTION OF ENTANGLEMENT FROM AN UNTRUSTED PARTY



## STEERING AS INFORMATION TASK

#### DISTRIBUTION OF ENTANGLEMENT FROM AN UNTRUSTED PARTY



- 1. A SENDS STATE TO B
- 2. B CHOOSES MEAS BASIS AND TELLS A
- 3. A GUESSES OUTCOME OF B

## STEERING AS INFORMATION TASK

#### DISTRIBUTION OF ENTANGLEMENT FROM AN UNTRUSTED PARTY



- 1. A SENDS STATE TO B
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WITH ENTANGLED STATE  $H(\sigma_{x}|A) + H(\sigma_{z}|A) = 0$ 

#### HOLDS FOR ANY CHEATING STRATEGY

STEERING INEQUALITY  $H(\sigma_{x}|A) + H(\sigma_{y}|A) \ge 1$ 

#### LOCAL UNCERTAINTY RELATION $H(\sigma_x) + H(\sigma_z) \ge 1$



#### STEERING INEQUALITIES

#### SUMMARY

#### 3 FORMS OF INSEPARABILITY IN QM



## 3 DIFFERENT CONCEPTS



DO WE TRUST MEAS. DEVICES OR NOT



 $\langle W \rangle_{o} \leq 0$  FOR ANY SEPARABLE  $\rho$ 



**ENTANGLEMENT** 





## DEVICE-INDEPENDENT QIP

**GOAL:** ACHIEVE INFORMATION-THEORETIC TASKS WITHOUT PLACING ASSUMPTIONS ON THE FUNCTIONING OF THE DEVICES USED IN THE PROTOCOL



NO ASSUMPTION ABOUT HILBERT SPACE DIMENSION OR ALIGNMENT OF MEASUREMENT DEVICES



**BELL INEQ VIOLATION**  $\implies$  TRULY RANDOM OUTCOMES

PIRONIO et al. NATURE 2010, COLBECK PhD 2007



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#### OUTCOMES CANNOT BE CORRELATED TO ANY OTHER PHYSICAL SYSTEM

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## DEVICE-INDEPENDENT Q CRYPTOGRAPHY



#### **BELL INEQUALITY VIOLATION**

#### LOCAL OUTCOMES ARE RANDOM AND UNCORRELATED FROM EVE

ACIN, NB, GISIN, MASSAR, PIRONIO, SCARANI PRL 2007

## DEVICE-INDEPENDENT Q CRYPTOGRAPHY



#### BELL INEQUALITY VIOLATION

#### LOCAL OUTCOMES ARE RANDOM AND UNCORRELATED FROM EVE

## SECURE EVEN IF EVE PREPARED THE DEVICES MORE ROBUST TO DEVICE IMPERFECTIONS

ACIN, NB, GISIN, MASSAR, PIRONIO, SCARANI PRL 2007

## EXPERIMENTS / LOOPHOLES

PRACTICAL IMPERFECTIONS OPEN LOOPHOLES

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PRACTICAL IMPERFECTIONS OPEN LOOPHOLES

## 1. LOCALITY LOOPHOLE $\rightarrow$ SPACE-LIKE SEPARATION

#### **OPTICAL EXPERIMENTS**

ASPECT et al. PRL 1982, TITTEL et al. PRL 1998, WEIHS et al. PRL 1998

## EXPERIMENTS / LOOPHOLES

PRACTICAL IMPERFECTIONS OPEN LOOPHOLES

## 1. **LOCALITY LOOPHOLE** $\rightarrow$ SPACE-LIKE SEPARATION

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# 2. **DETECTION LOOPHOLE** $\rightarrow$ HIGH DETECTION EFFICIENCY

#### ATOMIC EXPERIMENTS

ROWE et al. NATURE 2001, MATSUKEVITCH et al. PRL 2007
## PROGRESS (I)

#### BELL VIOLATION BETWEEN DISTANT IONS



 $CHSH = 2.19 \pm 0.09$ 

HOFMANN et al. SCIENCE 2012

## PROGRESS (II)

### LOOPHOLE-FREE STEERING



Total efficiency ~ 38% Steering ineq. violated by > 20  $\sigma$ 

WITTMANN et al. NJP 2012

## PROGRESS (III)

#### **NEW PROPOSALS**

#### ATOM-PHOTON ENTANGLEMENT NB et al. PRL 2007, CABELLO & LARSSON PRL 2007, TEO et al. Arxiv 2012

# CONTINUOUS VARIABLES

GARCIA-PATRON et al. PRL 2005, CAVALCANTI et al. PRA 2011

HIGHER DIMENSIONS VERTESI, PIRONIO, NB PRL 2010

HERALDED AMPLIFIER

GISIN, PIRONIO, SANGOUARD PRL 2010, CABELLO & SCIARRINO PRX 2012

## SUMMARY

### EXPERIMENTAL AND THEORETICAL PROGRESS TOWARDS LOOPHOLE-FREE BELL TEST



#### LAUNCH EXP. DEVICE-INDEPENDENT QIP

#### **NIST:** DI RANDOMNESS GENERATION

## NONLOCALITY BEYOND QM

## NONLOCALITY BEYOND QM



#### CAN WE HAVE CHSH = 4 ?

## NONLOCALITY BEYOND QM



#### CAN WE HAVE CHSH = 4 ?

 $E(X_0, Y_0) = E(X_0, Y_1) = E(X_1, Y_0) = 1$  AND  $E(X_1, Y_1) = -1$ 

## **IS CAUSALITY VIOLATED?**

 $E(X_0, Y_0) = E(X_0, Y_1) = E(X_1, Y_0) = 1$  AND  $E(X_1, Y_1) = -1$ 

## CAN WE HAVE CHSH = 4 ?



NONLOCALITY BEYOND QM

## POPESCU-ROHRLICH (PR) BOX



#### NONSIGNALING

MAXIMALLY NONLOCAL CHSH = 4

POPESCU & ROHRLICH 94, BARRETT et al. PRA 2005

## POPESCU-ROHRLICH (PR) BOX



#### NONSIGNALING

MAXIMALLY NONLOCAL CHSH = 4

#### WHY DOES THE PR BOX NOT EXIST IN NATURE ?

POPESCU & ROHRLICH 94, BARRETT et al. PRA 2005

## MACROSCOPIC LIMIT



BANCAL et al. PRA 2008

## MACROSCOPIC LIMIT



CHSH ~ 2 + 1/√M

MACROSCOPIC LIMIT (M  $\rightarrow \infty$ ) **LOCALITY** 

BANCAL et al. PRA 2008

## WITH PR BOXES



CHSH = 4 FOR ANY M !

NO MACROSCOPIC LIMIT NONLOCALITY AT ALL SCALES

NAVASCUES & WUNDERLICH 2010

## MACROSCOPIC LOCALITY

### **PRINCIPLE:** PHYSICAL CORRELATIONS BECOME LOCAL IN THE MACROSCOPIC LIMIT



#### MACROSCOPIC LOCALITY

NAVASCUES & WUNDERLICH 2010

## CONCLUSION

#### NONLOCALITY IS FUNDAMENTAL IN QM

#### ENTANGLEMENT VS NONLOCALITY ?

#### USEFUL FOR QIP $\rightarrow$ DEVICE-INDEPENDENT QIP

#### NEW PERSPECTIVE ON FOUNDATIONS OF QM

REVIEW ARTICLE : NB, CAVALCANTI, PIRONIO, SCARANI, WEHNER TO APPEAR SOON